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GIET UNIVERSITY, GUNUPUR – 765022
M. Sc. (First Semester) Examinations, March – 2023
22PHPC101 – Mathematical Methods in Physics
(Physics)

Time: 3 hrs

Maximum: 70 Marks

(The figures in the right hand margin indicate marks.)

PART – A**(2 x 10 = 20 Marks)****Q.1. Answer all questions**

	CO#	Blooms Level
a. Find $\int \frac{\sin z}{e^z - 1} dz$ where C is $ z + \pi = 2$	CO1	K2
b. Define singular point?	CO1	K1
c. State Laurent's theorem.	CO1	K1
d. Explain quotient law of tensor?	CO2	K1
e. Show that covariant derivative of δ^i_j is zero?	CO2	K1
f. Define cyclic group.	CO3	K1
g. What is Cayley's theorem in Group Theory?	CO3	K1
h. Prove that: $\epsilon_{ilm}\epsilon_{jlm} = 2\delta_{ij}$.	CO3	K2
i. Show the graph for Bessel polynomial $J_0(x)$ and $J_1(x)$?	CO4	K2
j. Derive Legendre polynomial $P_0(x)$ and $P_1(x)$?	CO4	K2

PART – B**(10 x 5 = 50 Marks)****Answer ANY FIVE questions**

	Marks	CO#	Blooms Level
2. State and Prove Taylors Theorem? Find the residue of the function $f(z) = \frac{z^2 - 2z}{(z+1)^2(z^2+4)}$	10	CO1	K1
3. Using Cauchy-Residue Theorem show that $\int_0^{2\pi} \frac{\cos 2\theta}{5+4\cos\theta} = \frac{\pi}{6}$	10	CO1	K2
4. Derive transformation laws for the Christoffel symbols of the first and second kind?	10	CO2	K1
5. Let G be an abelian group. Prove that the subset $H = \{g \in G : g^2 = e \text{ (identity element)}\}$ forms a subgroup of G.	10	CO3	K1
6. Show that for a finite group G, every representation is equivalent to a unitary representation.	10	CO3	K1
7.a. Prove that $\int_{-1}^1 \frac{P_n(x)}{\sqrt{(1-2xt+t^2)}} dx = \frac{2t^n}{2n+1}$ where n is a positive integer.	5	CO4	K2
b. Express $f(x) = x^3 + 2x^2 - x - 3$ in terms of Legendre polynomial?	5	CO4	K2
8. Derive the generating function of a Bessel polynomial?	10	CO4	K1

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