



**GIET UNIVERSITY, GUNUPUR – 765022**  
M. Sc. (First Semester) Examinations, March – 2023  
**22MTPC103 - Ordinary Differential Equation**  
(Mathematics)

Time: 3 hrs

Maximum: 70 Marks

(The figures in the right hand margin indicate marks.)

**PART – A**

(2 x 10 = 20 Marks)

**Q.1 Answer ALL questions**

- |   | CO# | Blooms Level |
|---|-----|--------------|
| a. Define Bernoulli Equation.   | CO1 | K2           |
| b. Find the differential equation of all circles touching a given straight line at a given point. | CO1 | K2           |
| c. Find the Wronskian of 1, x, $x^2$  | CO1 | K2           |
| d. Solve $p^2(x^2-a^2) - 2pxy + y^2 - b^2 = 0$  | CO2 | K2           |
| e. Find particular solution of $(D^3 - 2D)y = \cos 2x$  | CO2 | K2           |
| f. Solve $(D-1)(D^2 - D - 2)y = 0$  | CO2 | K2           |
| g. Solve $\left(D^3 - \frac{1}{x}D^2 + \frac{2}{x^2}D - \frac{2}{x^3}\right)y = 0$                | CO3 | K2           |
| h. Define variation of parameter method for solution of the linear differential equation.         | CO3 | K2           |
| i. Define Picard's method.  | CO4 | K2           |
| j. State Strum's separation theorem   | CO4 | K2           |

**PART – B**

(10 x 5 = 50 Marks)

**Answer ANY FIVE questions**

- |  | Marks | CO# | Blooms Level |
|--|-------|-----|--------------|
| 2. a. State and prove Abel's Formula   | 7     | CO1 | K2           |
| b. Find the differential equation of all circles of radius 'a'   | 3     | CO1 | K2           |
| 3.a. Solve the differential equation $\frac{dy}{dx} = \frac{x+y+4}{x-y-6}$   | 5     | CO1 | K2           |
| b. Solve the differential equation $(\cos y \sin 2x)dx + (\cos^2 y - \cos^2 x)dy = 0$  | 5     | CO1 | K2           |
| 4. a. Solve the differential equation $x^2 p^2 - 2xyp + y^2 - x^2 y^2 - x^4 = 0$   | 5     | CO2 | K2           |
| b. Solve $(D^6 - 64)y = e^{2x}$  | 5     | CO2 | K2           |
| 5.a. Solve $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 3y = \cos x + x^2$ by Undetermined Coefficient method   | 7     | CO2 | K2           |
| b. Solve the differential equation $\frac{(y-px)^2}{1+p^2} = a^2$  | 3     | CO2 | K2           |
| 6. a. Solve the Differential Equation $(D^2 + 3D + 2)y = x + \cos x$ by using variation of parameter   | 5     | CO3 | K2           |
| b. Solve $x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + y = \frac{\log x \sin \log x + 1}{x}$   | 5     | CO3 | K2           |
| 7. Solve the simultaneous differential equation  | 10    | CO3 | K2           |
| $\frac{dx}{dt} + \frac{dy}{dt} - 2y = 2\cos t - 7\sin t$ and $\frac{dx}{dt} - \frac{dy}{dt} + 2x = 4\cos t - 3\sin t$                          |       |     |              |
| 8. Apply Picard's method Find three successive approximations of the solution of $\frac{dy}{dx} = 2 - \left(\frac{y}{x}\right)$ , $y(1) = 2$ , | 10    | CO4 | K2           |

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