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GIET UNIVERSITY, GUNUPUR – 765022

B. C. A (First Semester) Examinations, March' 2023

BCA20104 – BASIC MATHEMATICAL COMPUTATION

Time: 3 hrs

Maximum: 70 Marks

The figures in the right hand margin indicate marks.

## PART – A: (Multiple Choice Questions)

(1 x 10 =10 Marks)

## Q. 1 Answer ALL questions

- |   | CO # | PO # |
|---|------|------|
| a. Find $x$ and $y$ . $[2x \ -y] + [y \ 3x] = 5[1 \ 0]$   | CO1  | PO1  |
| (i) $x = 1, y = 2$  |      |      |
| (ii) $x = 1, y = 3$   |      |      |
| (iii) $x = -1, y = 2$   |      |      |
| (iv) $x = 3, y = 1$   |      |      |
| b. The determinanat value of $\begin{vmatrix} 0.2 & 0.1 & 3 \\ 0.4 & 0.2 & 7 \\ 0.6 & 0.3 & 2 \end{vmatrix}$ is | CO1  | PO1  |
| (i) 0   |      |      |
| (ii) 1  |      |      |
| (iii) 0.2   |      |      |
| (iv) None of these  |      |      |
| c. The slope of the line joining the points (1,4) and (3,5) is  | CO2  | PO1  |
| (i) $\frac{1}{2}$   |      |      |
| (ii) $\frac{1}{3}$  |      |      |
| (iii) 2   |      |      |
| (iv) None of these  |      |      |
| d. The equation of tangent at (1,2) lying on the circle $x^2 + y^2 = 4$ .                                       | CO2  | PO1  |
| (i) $x + 2y = 4$  |      |      |
| (ii) $2x + y = 2$   |      |      |
| (iii) $x - 2y = 4$  |      |      |
| (iv) $2x + y - 2 = 0$   |      |      |
| e. Find $\lim_{(x,y) \rightarrow (2,1)} \left( \frac{x^2-4y}{x-2y} \right)$ is                                  | CO3  | PO1  |
| (i) 0   |      |      |
| (ii) 4  |      |      |
| (iii) 2   |      |      |
| (iv) Cant not find  |      |      |
| f. Find $f_x$ , where $f = \sin xy$   | CO3  | PO1  |
| (i) $y \cos xy$   |      |      |
| (ii) $x \sin xy$  |      |      |
| (iii) $y \cos x$  |      |      |
| (iv) 0  |      |      |
| g. Find the degree of the homogeneous function $ax^2 + by^2 + 2hxy$ is  | CO3  | PO1  |
| (i) -2  |      |      |
| (ii) 3  |      |      |
| (iii) 2   |      |      |
| (iv) 1  |      |      |
| h. Find the integration of $3^{2x}$   | CO4  | PO1  |
| (i) $\frac{3^{2x}}{3 \log a} + C$   |      |      |
| (ii) $\frac{3^{2x}}{2 \log 3} + C$  |      |      |
| (iii) $\frac{3^{2x}}{\log a} + C$   |      |      |
| (iv) None of these  |      |      |
| i. Find the value of $\int_0^1 x dx$ is   | CO4  | PO1  |
| (i) 0   |      |      |
| (ii) $\frac{1}{2}$  |      |      |
| (iii) 2   |      |      |
| (iv) None of these  |      |      |
| j. Compute $5! + 6!$ is   | CO1  | PO1  |
| (i) 840   |      |      |
| (ii) 320  |      |      |
| (iii) 110   |      |      |
| (iv) None of these  |      |      |

**PART – B: (Short Answer Questions)**

**(2 x 10 = 20 Marks)**

Q.2. Answer ALL questions

- |  |      |      |
|--|------|------|
| a. Find the Middle term of $(x^2 + a^2)^5$   | CO # | PO # |
| b. Find x,y .Where $\begin{bmatrix} 1 & 3 \\ 2 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \end{bmatrix}$ . | CO1  | PO2  |
| c. State Langranges’s Theorm.  | CO3  | PO1  |
| d. Verify the Euler’s theorm. Where $f=\cos^{-1}\frac{x}{y}$ .   | CO3  | PO2  |
| e. Find the $\int(a \tan x + b \cot x)^2 dx$   | CO4  | PO2  |
| f. Find the value of definite integral $\int_0^1 x e^{-x^2} dx$  | CO4  | PO2  |
| g. Find the equation of circle $x^2 + y^2 = 4$ which is inclined by $45^\circ$ with X-axis.  | CO2  | PO1  |
| h. Find the equation of straight line which passes through $(1, -2)$ and $(2, -3)$ .   | CO2  | PO1  |
| i. Find the derivative $\frac{dy}{dx}$ . Where $y = \sqrt{(\sin \sqrt{x})}$  | CO3  | PO2  |
| j. Construct the matrix of order $2 \times 3$ , where $a_{ij} = 2i + j$ .  | CO1  | PO2  |

**PART – C: (Long Answer Questions)**

**(10 x 4 = 40 Marks)**

Answer ALL questions

- |  | Marks | CO # | PO # |
|--|-------|------|------|
| 3.a. Find the Inverse of the matrix $A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$ .  | 5     | CO1  | PO2  |
| b. Show that $P(m,1)+P(n,1)=P(m+n, 1)$ for all positives integers.<br>(OR)   | 5     | CO1  | PO3  |
| c. Solve by Cramer’s rule $x + y + z = 4, 2x - y + 3z = 1, 3x + 2y - z = 1$  | 5     | CO1  | PO3  |
| d. Find the middle term of $(2x + \frac{1}{x})^9$ .  | 5     | CO1  | PO3  |
| 4.a. Find the angle between two straight lines $x - y = 0$ and $x + y = 0$   | 5     | CO2  | PO2  |
| b. Find the equation of the line passing through the point $(0,0)$ and $(-x_1, -y_1)$ .<br>(OR)  | 5     | CO2  | PO3  |
| c. . Show that ABC is a Isoscale triangle where $A(-3,1), B(5,4)$ and $C(0, -7)$   | 5     | CO2  | PO3  |
| d. Find the equation of the circle which passes through the points $(0,1) (1,0)$ and $(2,1)$ .   | 5     | CO2  | PO2  |
| 5.a. If $Z=x^2 + y^2 + 2xy$ , then prove that $xZ_x + yZ_y = 2Z$   | 4     | CO3  | PO3  |
| b. Find the tangent and normal of the curve $y = x e^{-x}$ at $x=0$<br>(OR)  | 6     | CO3  | PO2  |
| c. Find the total derivative $\frac{dU}{dt}$ where $U = \sin\left(\frac{x}{y}\right)$ $x = e^t$ and $y = t^2$ .                                      | 5     | CO3  | PO2  |
| d. Expand $2x^3 + 7x^2 + x - 6$ in the power of $(x - 2)$ .  | 5     | CO3  | PO3  |
| 6.a Find the Integration of $\int \frac{\sin x}{\sin(x+\alpha)} dx$  | 5     | CO4  | PO3  |
| b. .Find the area of the parabola $y^2 = 4ax$ bounded by its latus rectum $x = a$<br>(OR)  | 5     | CO4  | PO2  |
| c. Find the integration of i. $\int \frac{1-\cos 2x}{1+\cos 2x} dx$ ii. $\int (\tan x + \cot x)^2 dx$ iii. $\int \frac{\cos 2x}{\cos x + \sin x} dx$ | 6     | CO4  | PO3  |
| d. Find the Integration of i. $\int x \sin x dx$ ii. $\int x e^x dx$   | 4     | CO4  | PO3  |

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