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AR-18

M.SC

M.Sc 3rd SEMESTER REGULAR EXAMINATIONS, NOV/DEC 2019-20

Subject code: CC-PHY-301

Subject: Relativistic Quantum Mechanics & Field Theory

Time: 3 Hours

Max Marks: 80

The figures in the right hand margin indicate marks.

SECTION A

Q.1 Answer any four of the following: (4 x 4=16 Marks)

- a Discuss the drawbacks of Klein-Gordon equation. 4
- b Obtain Dirac equation for a free particle moving in a central field. 4
- c Express Dirac equation for a free particle in covariant form . 4
- d Explain gauge invariance with examples. 4
- e Derive the anti commutation relation $r^\mu r^\nu + r^\nu r^\mu = 2g^{\mu\nu} I$ for the Dirac gamma matrices. 4
- f Construct a suitable Lagrangian density for Dirac field. 4

OR

2. Answer all the questions from the following (2 x 8=16 Marks)

- a Write down the reasonings that led to the Dirac equation. 2
- b Discuss how negative energy was interpreted. 2
- c Discuss how the spin of electron came into existence and exist with two states. 2
- d Write Dirac matrices and explain why these are 4 x 4 matrices unlike pauli matrices which are 2 x 2. 2
- e What is improper Lorentz transformation? How it differs from proper Lorentz transformation? 2
- f Write down Dirac equation for an electron in electromagnetic field. 2
- g What are creation, annihilation and number operators? 2
- h Write down Lagrangian for charged scalar meson field. 2

SECTION-B

3. Answer all Questions: (16 x 4 = 64 Marks)

- a i) Derive Klein-Gordon equation for a relativistic particle and obtain continuity equation for its probabilities. Show that its probability density is not positive and definite. 8+8
- ii) Derive Dirac equation for a relativistic spin 1/2 particle and show that its probability



density is +ve and definite.

OR

- b i) Obtain Dirac matrices and establish their properties. 10+6
ii) Explain Dirac's Hole theory.
- 4a (i) Obtain the free particle solution of Dirac equation. 8+8
ii) Starting from Dirac equation for a free particle moving in a central field, obtain the expression for potential energy due to spin-orbit coupling.

OR

- b. Obtain Dirac equation for an electron in an e.m field. Reduce this equation into non-relativistic form and hence obtain an expression for magnetic moment of the electron. 16
- 5a i) Discuss the Lagrangian formulation of a continuous system as a limiting case a discontinuous system. 8+8
ii) Give an account of the Hamiltonian formulation of field theory and establish the equal time commutation relation for the fields.

OR

- b State and prove Noether's theorem for a Dirac field and hence derive the conservation of angular momentum from isotropy of space. 16
- 6a What is second quantization? Quantize the free Dirac field, explaining clearly the need for the equal time anti-commutation relation. 4+12

OR

- b Discuss the quantization of neutral scalar fields and obtain the expression of Hamiltonian in terms of creation and annihilation operators for real scalar field. 16