



## GIET MAIN CAMPUS AUTONOMOUS GUNUPUR – 765022

BD18001002

- g Determine whether the function is even or odd.  $f(x) = \log (x + \sqrt{x^2 + 1})$
- h Determine whether the function is even or odd.  $f(x)=x \left(\frac{a^{x}-1}{a^{x}+1}\right)$
- i Define hermitian and skew-hermitian matrix.
- j Check for Linear Dependent or linear independent of [3,0,2,2], [-6,42,24,54], [21,-21,0,-15]

## PART - C: (Long Answer Questions) 4X15=60 Marks

## Answer <u>ALL questions</u>

## Q.3 Expand $f(x, y) = x^2 + xy + y^2$ in powers of (x-2) and (y-3). а 7 8 b if $U = \tan^{-1} \frac{x^3 + y^3}{x - y}$ , $x \neq y$ then show that $x \frac{\partial U}{\partial x} + y \frac{\partial U}{\partial y} = \sin 2U$ OR Integrate $\int x^2 \sin 2x \cos 3x \, dx$ с 7 Verify $f_{xy} = f_{yx}$ where $f = e^{2x} \cos 3y$ d 8 Q.4 Solve $xy \frac{dy}{dx} = 1 + xy + x + y$ Solve y' + y = sin3x. 7 а 8 b OR Solve $y'' + 3y' - 18y = 9 \sin x$ by using undetermined coefficient method. Solve $3y'' + 10y' + 3y = 9x + 5 \cos x$ 7 с d 8 Q.5 Find the Fourier series of f(x) = x|x|, $-\pi < x < \pi$ . 7 а Find the Fourier series $f(x) = \frac{x^2}{2}$ in $-\pi < x < \pi$ 8 b OR Find the Half range sine Series of $f(x) = x^2$ , in $0 < x < \pi$ Find the Fourier series of $f(x) = \begin{cases} k, -\frac{\pi}{2} < x < \frac{\pi}{2} \\ 0, \frac{\pi}{2} < x < \frac{3\pi}{2} \end{cases}$ 7 с d 8 Q.6 Find the rank of the matrix $\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$ 7 а Solve the following system of equations by Gauss Elimination Method 8 b x + y - z = 9, 8y + 6z = -6, -2x + 4y - 6z = 40

cProve that the eigen values of a Hermitian matrix are Real.7dFind out which type of conic section is represented by Quadratic function8 $11 x^2 + 84 xy + 24 y^2 = 156$ 

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