

Fourth Semester Special Examination, 2012
COMPUTER BASED NUMERICAL METHOD

Time : 3 Hours

Full Marks : 70

Answer question No.1 which is compulsory and any five from the rest.
The figures in the right – hand margin indicate marks.

Q.1. Answer the followings

2X10

- Write the different sources of error in numerical computation.
- Explain the rate of convergence of regula falsi method
- What is the stability condition of a linear system of equations.
- Write the condition of convergence of Gauss Seidel method.
- Write the advantages and disadvantages of Lagranges method of interpolation.
- Find $\Delta^2 5, \nabla^2 8$ from the following data

x	0	2	4	6
y	2	5	8	14

- What is the error in Simpson's 3/8 rule.
- Explain predictor corrector method giving suitable example.
- Write Adam-Moulton predictor-corrector 3rd order formula to solve the initial value problem
- Write the error in Euler's modified method.

Q.2.a) Find the root of equation $\sin x - xe^x = 0$ using fixed point iteration method.

b) Find the rate of convergence of Newton-Raphson method to find the solution of an equation..

Q.3. a) Find the inverse of matrix $\begin{bmatrix} 1 & 10 & 1 \\ 10 & 1 & -1 \\ -1 & 1 & 10 \end{bmatrix}$ using Gauss Jordan method.

b) Solve the following system of equations using Gauss Jacobi method,

$$4x + y + 2z = 4$$

$$3x + 5y + z = 7$$

$$x + y + 3z = 3$$

Q.4. a) Find $f(0.5)$ and $f(3.5)$ using Newton divide difference interpolation method of the following data

x	-2	0	1	3	4
y	-23	1	4	82	193

b) Using inverse interpolation, find $f(6)$ of the following data

x	2	4	5
y	5	9	14

Q. 5. a) Find $f'(1)$, $f'(3)$ from the following data using Newton's finite difference method

x	-1	0	1	2	3
f(x)	0.333	1	3	9	27

b) Evaluate $I = \int_1^2 \frac{2x^2}{1+x^4} dx$, using Simpson's 3/8 rule.



Q.6 .a) Evaluate $I = \int_0^{\pi/2} \sin x dx$, using Simpson's 3/8 rule.

b) Evaluate $I = \int_{-1}^1 e^x \cos x dx$ using Gauss 3-point formula.

Q. 7. a) Solve $dy/dx = y + x^2$, $y(0)=1$ using Taylor's series method in the interval $[0, 0.4]$.

b) Find the value of $y(1.2)$ where $dy/dx = \sqrt{x+y}$, $y(0.4)=0.41$ using Modified Euler's Method

Q.8.a) Write the algorithm to find the solution of a differential equation using Runge-Kutta method of 4th order.

b) Write the algorithm to solve the following equation by using Adam-Bashforth 3rd order method

$$dy/dx = \frac{1}{1+x^2}, y(0) = 1 \text{ in the interval } [0, 1].$$