

First Semester Special Examination – 2012  
MECHANICS (OLD COURSE)

Full Marks – 70

Time – 3 Hours

Answer Question No. 1 which is compulsory and any five from the rest.  
The figures in the right-hand margin indicate marks.

1. Answer the following questions: 2×10
  - (a) In a concurrent force system, two forces are acting on a point at an angle  $60^\circ$ . The resultant force is 80 kN and one of the forces is 30 kN. Determine the other force.
  - (b) Explain 'free body diagram' with an example.
  - (c) State the laws of friction.
  - (d) Differentiate between active forces and reactive forces.
  - (e) Explain virtual work.
  - (f) Why the trajectory of a projectile is a parabola?
  - (g) Define centre of mass and centre of gravity.
  - (h) What is the relation between impulse and momentum?
  - (i) State and explain law of conservation of energy.
  - (j) What do you mean by plane curvilinear motion?
  
2.
  - (a) Explain what do you mean by concurrent forces in a plane. What is the condition for equilibrium of concurrent forces in a plane? (5)
  - (b) Locate the centroid of the area enclosed between a straight line  $y = 2x$  and the parabola  $y^2 = 4x$ . (5)
  
3. (a) A smooth circular cylinder of radius 2 m is lying in a triangular groove, one side of which makes  $20^\circ$  angle and the other  $50^\circ$  angle with the horizontal. Find the reactions at the surfaces of contact, if there is no friction and the cylinder weighs 100 kN. (6)

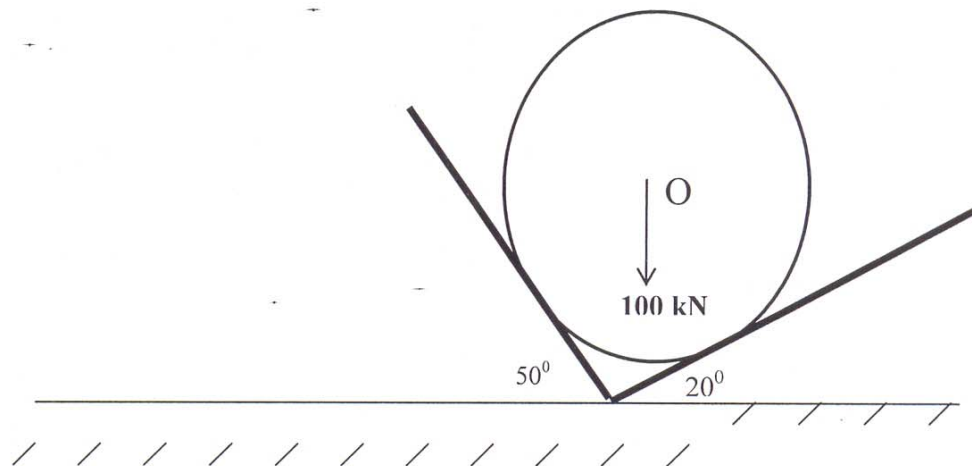


Figure 1

- (b) Two men carry a weight of 25 kN by means of two ropes fixed to the weight. One rope is inclined at  $40^\circ$  and the other at  $25^\circ$  with the vertical. Find the tension in each rope. (4)

4.(a) State and explain Pappus theorem with neat diagrams. (5)

(b) A spring gun, having a spring constant of  $4 \text{ N/mm}$  is held on a vertical position. If the original compression of the spring is  $200 \text{ mm}$ , how high above its compressed position will it project a ball of weight  $20 \text{ N}$ ? What will be the velocity of the ball at a height of  $2 \text{ m}$ ? (5)

5. Find the polar moment of inertia at the centroid of the L section shown in Figure 2. The section has a thickness of  $30 \text{ mm}$  throughout. (10)

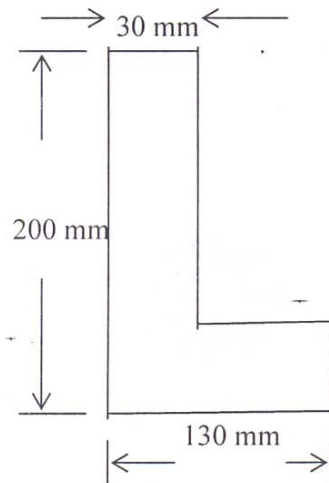


Figure 2

6.(a) An  $80 \text{ kg}$  man sits in a  $50 \text{ kg}$  canoe and fires a  $100 \text{ gm}$  bullet horizontally directly over the bow of the canoe. Neglecting friction of water, find the velocity ' $v$ ' with which the canoe will move after the shot if the rifle has a muzzle velocity of  $500 \text{ m/s}$ . (5)

(b) Two adjacent guns having the muzzle velocity of  $400 \text{ m/s}$  fire simultaneously at an angle and for the same target at a range  $5000 \text{ m}$ . Calculate the time difference between the hits. (5)

7.(a) A ball of mass  $m$  is dropped on to a spring of stiffness  $k$  from a height  $h$ . Find the deflection of the spring if the ball is brought to rest. (5)

(b) A bullet moving at the rate of  $300 \text{ m/sec}$  is fired into a thick target and penetrates  $0.6$  meters. If it is fired with same velocity into a  $0.25 \text{ m}$  thick target, find the velocity of emergence. Assume the resistances to be uniform in both the cases. (5)

8. Write short notes of the followings (2.5x4)

- (a) Method of joints
- (b) Angular velocity
- (c) D' Alembert's Principle
- (d) Angle of friction and angle of repose.