

Or

(b) Explain the significance of Hamilton's principal function and discuss the Kepler's problem using Hamilton-Jacobi method.

6. (a) Discuss method of small oscillations and using this method derive an equation for the frequency of a two coupled oscillator.

Or

(b) Give the general theory of Small oscillators and discuss the normal modes of vibration.

2019**(January)***Time : 3 hours**Full Marks : 80*

Answer from both the Sections as per direction

The figures in the right-hand margin indicate marks

Candidates are required to answer in their own words as far as practicable

(CLASSICAL MECHANICS)**SECTION – A**

1. Answer any *four* of the following : 4 × 4

(a) Write a note on infinitesimal rotations.

(b) Explain torque free motion of a rigid body.

(c) State and explain variational principle.

(d) Explain the principle of least action.

(e) Explain Hamilton-Jacobi theory.

(2)

(f) Discuss the normal coordinates of vibration.

Or

2. Answer *all* questions from the following : 2×8

(a) Define Eulerian angles.

(b) Define symmetrical top.

(c) Give the importance of Legendre transformations.

(d) Define inertia tensor.

(e) What do you mean by integral invariance ?

(f) Explain action angle variables.

(g) Define small oscillations.

(h) Explain the terms normal modes and normal coordinates.

SECTION – B

Answer all questions : 16×4

(3)

3. (a) Define coriolis force and obtain the kinetic energy of rotations of a rigid body with respect to the principal axes in terms of the Euler's angles.

Or

(b) Discuss in detail the motion of heavy symmetrical top having a fixed point and obtain the condition for a slipping top.

4. (a) Explain the techniques of calculus of variations Lagrange's equations from Hamilton's principle.

Or

(b) Give the physical significance of Hamiltonian and obtain the Hamilton's equations of motion from a variational principle.

5. (a) State and explain Poisson's theorem and show that the poisson bracket is invariant under canonical transformation.