



# GIET Main Campus (Autonomous)

## Gunupur-765 022

Reg.No.: 

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**B.TECH. DEGREE EXAMINATION-NOV-DEC-2018**

**End Semester Examination**

**BBSBS3040-Engineering Mathematics-III**

**(Regulations 2017)**

**Time : 3 Hours**

**Maximum : 100 Marks**

**Question Code:10812**

**Answer ALL Questions**

**PART A - (10 X 2 = 20 Marks)**

- 1 a) The modulus and argument of  $z = \sqrt{3}$  is \_\_\_\_\_. [CO1][PO1]
- a)  $\sqrt{3}$
- b)  $-\sqrt{3}$
- c) 3
- d) -3
- b) An Analytic function with constant modulus is \_\_\_\_\_. [CO1][PO1]
- a) real
- b) imaginary
- c) constant
- d) none of the these
- c) The order of zero of the function  $f(z) = (z - 2)^3$  is \_\_\_\_\_. [CO2][PO1]
- a) 2
- b) 3
- c) 0
- d) 4
- d) The negative powers of the Laurent series is called \_\_\_\_\_. (CO2)[PO1]
- a) Analytic part
- b) principal part
- c) Taylor's part
- d) none of these



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- e) The Residue of  $\frac{e^{2z}}{z^2}$  is: \_\_\_\_\_. [CO2][PO1]  
a) 3  
b) 0  
c) -1  
d) 2
- f) Newtn's forward interpolation is used for \_\_\_\_\_. [CO3][PO1]  
a) equal interval  
b) unequal interval  
c) both the intervals  
d) none of these
- g) The order of error of simpson's one third rule is \_\_\_\_\_. [CO3][PO1]  
a) ) order h4  
b) order h3  
c) order h2  
d) none of these
- h) Two events are Mutually Exclusive if they have \_\_\_\_\_. [CO4/PO1]  
a) independent  
b) dis joint  
c) common element  
d) non of these
- i) The value of correlation coefficient lies between \_\_\_\_\_. [CO4/PO1]  
a) 0 to 1  
b) b) -1 to 0  
c) c) -1 to 1  
d) d) none of these
- j) The mean and variance of \_\_\_\_\_ distribution are equal. [CO4/PO1]  
a) Bionomial  
b) poision  
c) Normal  
d) uniform



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PART B - (10 X 2 = 20 Marks)

- 2 a) Solve  $z = \sqrt[4]{-i}$  [ CO1][PO2]
- b) Verify whether the function is Analytic or not.  $F(z) = z^3$  [ CO1][PO1]
- c) Define Laurent series of a function  $f(z)$ . [ CO2][PO1]
- d) Find the Residue at the singular point  $f(z) = \frac{z}{z^2+9}$  [ CO2][PO1]
- e) Discuss the nature of singularity of  $\frac{1}{\cos z - \sin z}$  [ CO2][PO1]
- f) What is rounding off error? Explain with an example [ CO3][PO1]
- g) Define Newton's forward difference interpolation formula. [ CO3][PO1]
- h) Prove that  $P(A \cup B) = P(A) + P(B) - P(AB)$  [ CO4][PO2]
- i) Define conditional probability [ CO4][PO1]
- j) Find the mean of the random variable  $x$ , its probability function is

$$f(x) = \binom{3}{x}, x=0,1,2,3 \quad [ CO4/PO2 ]$$



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PART C - (4 X 15 = 60 Marks)

- 3 a i) Verify whether the function satisfies harmonic . if yes find its conjugate harmonic  
 $v = \tan^{-1} \frac{y}{x}$ . [CO1][PO2] [7]

- ii) Evaluate  $\oint_c \frac{z^2 dz}{z^4 - 1}$ ,  $c: |z + 1| = 1$  [CO1][PO2] [8]

(OR)

- b i) Find the line integral over the curve  $\oint_c z dz$ ;  $c: x^2 = y$  from 0 to 1+i [CO1][PO2] [8]

- ii) Evaluate  $I = \int Re z^2 dz$ , where 'c' is the boundary of square with vertices 0, 1, 1+i, i .in clockwise. . [CO1][PO2] [7]

- 4 a i) Find the Laurent series of  $\frac{z^2}{(z-1)(z-2)}$ , valid in the region  $1 \leq |z| \leq 2$ . [CO2][PO2] [8]

- ii) Evaluate  $\oint \frac{e^z + z}{z^3 - z} dz$   $c: |z| = \frac{\pi}{2}$  by residue theorem. [CO2][PO2] [7]

(OR)

- b i) Evaluate  $\oint \frac{z+1}{(z^2+4)^2} dz$ ,  $c: |z| = \frac{2\pi}{3}$  by residue theorem. [CO2][PO2] [8]

- ii) Solve the integral  $\int_{-\infty}^{\infty} \frac{1}{(z^2+2)^2} dz$ . [CO2][PO2] [7]

- 5 a i) Evaluate  $\int_0^1 \frac{dx}{1+x^2}$  using Trapezodial Rule with  $h=0.2$ . [CO3][PO2] [7]

- ii) Find  $y(1.2)$  by modified Euler's method given  $\frac{dy}{dx} = \frac{2y}{x} + x^3, y(1)=0.5$  [CO3][PO2] [8]

(OR)

- b i) Calculate  $y(0.1), y(0.2)$  using RK method given that

$$\frac{dy}{dx} = \frac{2xy}{1+x^2} + 1, y(0) = 0 \quad [CO3/PO2] [8]$$

- ii) Find the real roots of  $x^3 + x - 5 = 0$ , upto four significant figure by iteration method. [CO3][PO2] [7]

- 6 a i) A random variable X has the following probability function [CO4/PO2] [8]

Values of X:	1	2	3	4	5
P(x):	k	k	k	3k <sup>2</sup>	k <sup>2</sup>



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- a) Find  $k$     b) Compute  $P(x < 4)$     c) Compute  $p(x > 3)$     d) Find  $p(1 < x < 4)$   
ii) Find the regression line  $X$  on  $Y$  in the points  $(1, -3), (2, -11), (3, 1), (4, 18), (5, 61), (6, 11)$

[ CO4/PO2 ][7]

(OR)

- b i) Find the regression line  $X$  on  $Y$  in the points  $(1, -3), (2, -11), (3, 1), (4, 18), (5, 61), (6, 11)$

[ CO4][PO2 ][8]

- ii) Apply the maximum likelihood method to the Normal distribution with  $\mu=0$ .

[ CO4][PO2 ][7]