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Total Number of Pages: 2

B.TECH
PAT2A001

2nd Semester Regular / Back Examination 2016-17
Applied Mathematics-II
BRANCH: All
Time: 3 Hours
Max Marks: 100
Q.CODE: Z337

Answer Part-A which is compulsory and any four from Part-B.
The figures in the right hand margin indicate marks.

Part – A (Answer all the questions)

Q1 Answer the following questions: dash fill up type (2 x 10)

- Laplace transform of $e^t \cosh 3t =$ _____
- Inverse Laplace transform of $\frac{5s}{s^2 - 25} =$ _____
- Laplace transform of $4u(t - \pi) \cos t =$ _____
- The period of the function $\cos\left(\frac{3\pi x}{2}\right) =$ _____
- The derivative of $\vec{F}(t) = te^t \hat{i} + t^2 \hat{j} + \sin t \hat{k} =$ _____
- If $\vec{F} = xyz(x\hat{i} + y\hat{j} + z\hat{k})$ then $\vec{\nabla} \cdot \vec{F} =$ _____
- If $\vec{F} = x\hat{i} + 2y\hat{j} - z\hat{k}$ then $\vec{\nabla} \cdot (\vec{\nabla} \times \vec{F}) =$ _____
- For the surface $4x^2 + 9y^2 = 1$ write down the parametric expression $\vec{r}(u, v)$
: _____
- The Fourier series for the function $\sin^2 x =$ _____
- The value of $\beta(3, 4) =$ _____

Q2 Answer the following questions: Short answer type (2 x 10)

- Find the constant term in the Fourier series for the function $f(x) = x^2$, with period 2π .
- Evaluate $\int_0^2 \int_0^1 x \, dx \, dy$
- Find out the unit surface normal to the surface of the cone $\vec{r}(u, v) = u \cos v \hat{i} + u \sin v \hat{j} + cu \hat{k}$.
- Find the curl of the function $\vec{F} = xyz(x\hat{i} + y\hat{j} + z\hat{k})$.
- Find the length of the curve $\vec{r}(t) = \cos t \hat{i} + \sin t \hat{j} + t \hat{k}$ from $(1, 0, 0)$ to $(1, 0, 2\pi)$.
- Find the directional derivative of the function $f = xyz$ at $(-1, 1, 3)$ in the direction $\vec{a} = \hat{i} - 2\hat{j} + 2\hat{k}$.
- Using the value $\Gamma(0.5) = \sqrt{\pi}$, compute $\Gamma(-3.5)$.

- h) Find the Laplace transform of $f(t) = \begin{cases} t, & 0 < t < 2 \\ 0, & \text{otherwise} \end{cases}$.
- i) Find the inverse Laplace transform of $\frac{3}{s^2 + 6s + 18}$.
- j) Find the inverse Laplace transform of $\ln \frac{s+a}{s+b}$.

Part – B (Answer any four questions)

- Q3 a) Solve $y'' + y = 2 \cos t$, $y(0) = 3$, $y'(0) = 4$ using Laplace transform. (10)
- b) Find the inverse Laplace transform of $\frac{3(1 - e^{-\pi s})}{s^2 + 9}$. (5)
- Q4 a) Solve $y'' + 4y = r(t)$, $r(t) = 1$ if $0 < t < 1$ & 0 if $t > 1$, $y(0) = 1$, $y'(0) = 0$. (10)
- b) Solve $y(t) = 1 + \int_0^t y(\tau) d\tau$. (5)
- Q5 a) Show that $\left[\int_0^\infty x e^{-x^8} dx \right] \times \left[\int_0^\infty x^2 e^{-x^4} dx \right] = \frac{\Gamma(0.5)\Gamma(0.75)}{32}$ (10)
- b) Evaluate $\int_C \vec{F} \cdot d\vec{r}$ where $\vec{F} = xy\hat{i} + x^2y^2\hat{j}$, $C: y = x^2$, from $(0,0)$ to $(1,4)$ (5)
- Q6 a) Evaluate $\int_0^{\pi/4} \int_x^{\pi/4} \frac{\sin y}{y} dy dx$ (10)
- b) Find the area enclosed by the cardioids $r = a(1 - \cos\theta)$ (5)
- Q7 a) Evaluate $\iint_S \vec{F} \cdot \hat{n} dA$ where (10)
- $\vec{F} = x\hat{i} + y\hat{j} + z\hat{k}$, $S: \vec{r} = u \cos v \hat{i} + u \sin v \hat{j} + u^2 \hat{k}$, $0 \leq u \leq 4$, $-\pi \leq v \leq \pi$
- b) Evaluate $\iint_S \vec{F} \cdot \hat{n} dA$ by using divergence theorem where (5)
- $\vec{F} = \cos y \hat{i} + \sin x \hat{j} + \cos z \hat{k}$, $S: \text{the surface of } x^2 + y^2 \leq 4, |z| \leq 2$
- Q8 a) Find the Fourier series of the function $f(x) = \begin{cases} 0 & -1 < x < 0 \\ x & 0 < x < 1 \end{cases}$ with (10)
- period 2.
- b) Find the Fourier sine series of the function $f(x) = \pi - x$, $0 \leq x \leq \pi$. (5)
- Q9 a) Find the Fourier cosine integral of $f(x) = e^{-x} + e^{-2x}$, $x > 0$. (10)
- b) Find the Fourier transform of the function $f(x) = 1$, $a < x < b$, 0 otherwise. (5)