

Registration No.

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Total number of pages : 04

B.Tech.
PCE61101

6th Semester Regular Examination 2017-18

NUMERICAL METHODS & MATLAB

BRANCH : CHEM

Time : 3 Hours

Max Marks : 100

Q.CODE : C141

Answer Part-A which is compulsory and any four from Part-B.

The figures in the right-hand margin indicate marks.

Assume suitable notations and any missing data wherever necessary.

Answer all parts of a question at a place.

Part – A (Answer all the questions)

Q1. Answer the following questions : (2 x 10)

(a) _____ is used to denote the process of finding the values inside the interval (X_0, X_n) .

- Interpolation
- Extrapolation
- Iterative
- Polynomial equation

(b) Lagrange's interpolation formula is used to compute the values for _____ intervals.

- Equal
- Unequal
- Open
- Closed

(c) Romberg's method is also known as _____.

- Trapezoidal rule
- Simpson's (1/3)rd Rule
- Simpson's (3/8)th Rule
- Rombergs Integration

(d) In Simpson's 1/3rd rule the number of intervals must be _____.

- A multiple of 3
- A multiple of 6
- Odd
- Even

(e) The Eigenvalues of $\begin{bmatrix} 5 & 6 & 17 \\ 0 & -19 & 23 \\ 0 & 0 & 37 \end{bmatrix}$ are

- 37, 5, -19
- 37, -5, 19
- 7, -3, 2
- 37, -5, 3

(f) The Eigen values of a 4×4 matrix [A] are given as 2, -3, 13, and 7. The det(A) is _____.

- 546
- 19
- 25
- Cannot be determined

- (g) $y(x+h) = y(x) + h f(x,y)$ is referred as _____ method.
- Euler
 - Modified Euler
 - Taylor's Series
 - Runge-Kutta
- (h) The power method for approximating Eigen value is _____ method.
- Iterative
 - Point-wise
 - Direct
 - Indirect

(i)

$$5 \frac{\partial^2 z}{\partial x^2} + 6 \frac{\partial^2 z}{\partial y^2} = xy$$

The partial differential equation is classified as

- Elliptic
 - Parabolic
 - Hyperbolic
 - None of these
- (j) A partial differential equation requires
- Exactly one independent variable
 - Two or more independent variables
 - More than one dependent variable
 - Equal number of dependent and independent variables

Q2. Answer the following questions : (2 x 10)

- (a) If $Y(X_i) = Y_i, i=0, 1, 2, \dots, n$ write down the formula for the cubic spline polynomial $Y(X)$ valid in $X_{i-1} \leq X \leq X_i$.
- (b) What is interpolation? What is the difference between interpolation and extrapolation?
- (c) State Forward divided difference formula for finding $F'(x)$ and $f''(x)$.
- (d) The table given below reveals the velocity v of a body during the time t specified. Find its acceleration at $t=1.1$.

| | | | | | |
|-----------|------|------|------|------|------|
| T(in sec) | 1.0 | 1.1 | 1.2 | 1.3 | 1.4 |
| V(in m/s) | 43.1 | 47.7 | 52.1 | 56.4 | 60.8 |

- (e) Define Discrete Fourier Transform and algebraic form of FFT.
- (f) Find a QR factorization of a matrix $\begin{bmatrix} 3 & 7 \\ 4 & 4 \end{bmatrix}$.
- (g) What is the need of numerical solution for differential equations?
- (h) "Multistep methods are not self-starting". Justify.
- (i) State the condition of the equation $Au_{xx} + Bu_{yy} + Cu_{xy} + Du_x + Eu_y + Fu = G$ where A, B, C, D, E, F, G are functions of x and y to be (i) elliptic (ii) parabolic (iii) hyperbolic.
- (j) Write down Adam-Bashforth predictor formula.

Part – B (Answer any four questions)

- Q3. (a)** The following table gives some relationship between steam pressure and temperature. Find the pressure at temperature 372 using piecewise linear interpolation. **(04)**

| | | | | | |
|---------------|-------|-------|-------|-------|-------|
| T(K) | 361 | 367 | 378 | 387 | 399 |
| P(kPa) | 154.9 | 167.9 | 191.0 | 212.5 | 244.2 |

- (b)** Find the second derivative at $x=4$, using the following data: **(03)**

| | | | | |
|----------|---|---|---|----|
| x | 0 | 2 | 4 | 6 |
| y | 2 | 5 | 8 | 14 |

- (c)** Find the values of $f''(0.2)$, $f''(0.6)$, $f''(1.0)$ from the following data using appropriate initial values based on finite difference and Richardson's extrapolation method. **(08)**

| | | | | | |
|-------------|------|------|------|------|------|
| x | 0.2 | 0.4 | 0.6 | 0.8 | 1.0 |
| F(x) | 0.12 | 0.49 | 1.12 | 2.02 | 3.20 |

- Q4. (a)** **(05)**

Compute $I = \int_0^{\frac{\pi}{3}} \tan x dx$, using Simpson's rule with $h=\pi/6, \pi/12, \pi/24$ and then by Romberg's method.

- (b)** Using Hermite's interpolation formula estimate the value of $\ln 3.2$ from the following data **(10)**

| | | |
|----------|-----------------|------------------|
| x | F(x)=lnx | F'(x)=1/x |
| 3.0 | 1.09861 | 0.33333 |
| 3.5 | 1.25276 | 0.28571 |
| 4.0 | 1.38629 | 0.25 |

- Q5. (a)** Find the dominant Eigen value of the following matrix by power method and compare with Rayleigh's quotient method. **(10)**

$$A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$

- (b)** The differential equation $\frac{dy}{dx} = y - x^2$ satisfied by $y(0)=1, y(0.2)=1.1218, y(0.4)=1.4282, y(0.6)=1.7379$. Compute $y(0.8)$ by Milne's predictor-corrector method. **(05)**

- Q6. (a)** Find the QR factorization of the matrix $\begin{bmatrix} 1 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}$ using Gram Schmidt process. **(10)**

- (b)** Compute 4-point DFT of the following sequence using DIT and DIF algorithms. **(05)**
 $X(n) = \{0, 1, 2, 3\}$

Q7. Find the numerically smallest Eigen value of the matrix A by finding A^{-1} and without finding A^{-1} given that one of the Eigen values of A is -20. **(15)**

$$A = \begin{bmatrix} -15 & 4 & 3 \\ 10 & -12 & 6 \\ 20 & -4 & 2 \end{bmatrix}$$

Q8. Solve $25u_{xx} - u_{tt} = 0$ for u with the boundary conditions $u(0,t) = 0, u(5,t) = 0$ and the initial conditions $u_t(x,0) = 0$ and $u(x,0) = 2x$ for $0 \leq x \leq 2.5$ $u(x,0) = 10 - 2x$ for $2.5 \leq x \leq 5$, taking $h = 1$. (for four time steps) **(15)**

Q9. (a) Given $\frac{\partial^2 f}{\partial x^2} = \frac{\partial f}{\partial t}$, **(05)**

Subject to $f(0,t) = f(5,t) = 0, f(x,0) = x^2(25 - x^2)$.
Find f in the range taking $h = 1$ and up to 5 seconds.

(b) Solve $\nabla^2 u = -10(x^2 + y^2 + 10)$ over the square mesh with sides $x = 0, y = 0, x = 3, y = 3$ with $u = 0$ on the boundary and mesh length is 1 unit. **(10)**