Registr	ation No :
	umber of Pages: 03 B.Tech. PMA4E001
210	4 th Semester Regular / Back Examination 2017-18
	APPLIED MATHEMATICS – III BRANCH : AEIE, AERO, AUTO, BIOMED, BIOTECH,
CIV	'IL, CSE, ECE, EEE, EIE, ELECTRICAL, ENV, ETC, FAT, IEE, IT, MANUFAC,
MAN	JTECH, MECH, METTA, MINERAL, MINING, MME, PE, PLASTIC, PT, TEXTILE
	Time : 3 Hours Max Marks : 100
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	Answer Part-A which is compulsory and any four from Part-B.
	The figures in the right hand margin indicate marks. Answer all parts of a question at a place.
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Q1	Part – A (Answer all the questions) Answer the following questions: multiple type or dash fill up type: (2 x 10)
a)	Let $f(z)$ and $g(z)$ has pole of order '20' and '18'at $z = 1$ respectively then what
210	is the order of pole of the function $f(z) \times g(z)$ at $z = 1$
b)	(a) 36 (b) 38 (c) 2 (d) -2 If $f(z)$ has removal singularity at $z = \infty$, then $f(z)$ is equal to
b)	(a) $\sin z$ (b) $\cos z$ (c) $\tan z$ (d) none
c)	If both real part and imaginary part of a complex function are harmonic
	conjugate to each other then the function must be (a) Analytic (b) Differentiable (c) constant (d) none
²¹⁰ d)	
,	(a) Removal singular point (b) Isolated essential singular point
	(c) pole (d) non isolated essential singular point
e)	Simpson's rule is exact for a polynomial of degree
f)	(a) 5 (b) \leq 5 (c) 2 (d) \leq 2 Let $\frac{dy}{dx} = -2xx^2 x(0) = 1$ with step size $h = 0.2$ then by Euler method the value
-,	Let $\frac{dy}{dx} = -2xy^2$, $y(0) = 1$ with step size h = 0.2 then by Euler method the value of $y(0.4)$ is
²¹⁰ g)	Using Lagrange interpolation how many nodes or arguments are required to
	obtain a polynomial of degree 10
h)	(a) 11 (b) 12 (c) 21 (d) 10 Two dice are rolled, the probability of even doublet occur on the surface is
,	?
i)	Let the cumulative distribution function of the random variable X is given by $x = 0$
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	$F(x) = \begin{cases} \frac{2x}{x}; & 0 \le x < \frac{1}{2} \\ \frac{1+x}{2}; & \frac{1}{2} \le x < 1 \end{cases}$ Then $P(X = \frac{1}{2}) = \frac{210}{210}$?
	$\begin{pmatrix} 2 & 2 & 2 & 3 \\ 1; & x \ge 1 \end{pmatrix}$
j)	The distribution function of random variable X is given by
	$\begin{cases} cx^3 ; 0 \le x < 3 \\ 1 : x > 3 \end{cases}$
	$F(x) = \begin{cases} 2x & 0 \le x < 3 \\ 1; & x \ge 3 \\ 0; & x < 0 \end{cases}$ Then $c = $?
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(5)

Find the Radius of convergence of $\sum_{n=0}^{\infty} a_n z^n$ where

$$a_n = \begin{cases} \left(\frac{1+i\sqrt{3}}{2}\right)^n, & \text{is even} \\ \left(\frac{1-i}{3}\right)^n, & \text{is odd} \end{cases}$$

- Evaluate $\int_{c:|z|=3} \frac{e^{2z}dz}{(z+1)^4}$
- c) Find the principal value of $(-1)^{\frac{-5i}{\pi}}$. d) Residue of $f(z) = \frac{\sin z z}{z^3}$ at z = 0 is _____.
- e) What is the approximate value of $\int_0^1 \frac{x}{x+1} dx$ by Simpson's rule?
- If $p(x) = 2 + \alpha(x+1) + x(x-\beta)$ interpolates the points (x,y) in the table

х	-1	0	1
у	2	1	2

Then
$$+\beta \stackrel{\text{210}}{=}$$

- Find the unique polynomial of degree ≤ 2 such that f(0) = 1, f(1) = 3 and
- Fit a straight line using the following data y = a + bx

X	0	1	2	3	4
У	1	1.8	3.3	4.5	6.3

- The Random variable X can takes on two values 2 and 4, where i) P(X=2) = 0.2 and P(X=4) = 0.8 then find $E(X^2)$.
- j) What is the probability mass function of poisson distribution?

Q3 a) Evaluate
$$\oint_{|z|=4} \frac{\cos z \, dz}{z^2(z-\pi)^2}$$
 by Residue theorem. (10)

b) Find the analytic function
$$f(z) = u + iv$$
 whose real part $u = e^{-2x} \sin 2y$. (5)

Q4 a) Show that
$$\int_{-\infty}^{\infty} \frac{dx}{1+x^4} = \frac{\pi}{\sqrt{2}}$$
 by contour method. (10)

b) Evaluate the contour integration
$$\int_0^{2\pi} \frac{1+2\cos\theta}{5+4\cos\theta} d\theta$$
 (5)

Find the interpolating polynomial and an approximation to the value of f(10) (10)Q5 using the following data points

X	0.5	1.5	3.0	5.0	6.5	8.0
f(x)	1.625	5.875	31.000	131.000	282.125	521.0

Find tan(0.12) using the following data points

X 210	0.10	0.15	0.20	0.25	0.30
y=tan x	0.1003	0.1511	0.2027	0.2553	0.3093

b) Evaluate $\int_0^2 \frac{dx}{x^2+4}$ using Simpson's rule and Romberg's method for step size h_0 (5) = 0.5

(10)

- **Q7** a) Expand $f(z) = \frac{1}{z^2 3z + 2}$ in the following regions (10)
 - (a) 0 < |z| < 1 (b) 1 < |z| < 2 (c) |z| > 2
 - **b)** Let R be the radius of convergence of $\sum_{n=0}^{\infty} a_n z^n$ then find the radius of convergence of (a) $\sum_{n=0}^{\infty} (a_n^{210})^2 z^n$ (5)
- Q8 a) If the mathematics scores of BPUT examination are normal with mean 70 and standard deviation 20 and if some companies sets 75 as the minimum score for qualifying to sit in campus drive, then what percent of students will not reach that score.
 - **b)** A continuous Random variable X, has the probability density function (5)

 $f(x) = \begin{cases} \frac{2x}{R^2}; & 0 < x < R \\ 0; & \text{Otherwise} \end{cases}$ then find the Mean and Variance of the distribution.

Q9 a) Find the equations of two lines of regression for the following data .Also obtain the estimation of X for Y= 54

X	27	25	22	20	18	17	16
Υ	2700	69	2 68	62 ₂	_{1.} 56	54 ₂	₁₀ 50

b) A normally distributed random sample of size 100 observations is taken from its population with standard deviation 8 and unknown mean μ . A statistician uses the critical region $\bar{x} > 43$ for testing the null Hypothesis $H_0: \mu = 41$. Calculate power of the test w.r.t. alternate hypothesis H: $\mu = 42$