



Gandhi Institute of Engineering and Technology University, Odisha, Gunupur
(GIET UNIVERSITY)

M.Sc. (First Semester - Regular) Examinations, January - 2026
24MPHPC11004 – Quantum Mechanics-I
(Physics)

Time: 3 hrs

Maximum: 60 Marks

(The figures in the right hand margin indicate marks)

PART – A**(2 x 5 = 10 Marks)**Q.1. Answer **ALL** questions

- | | CO # | Blooms Level |
|-------------------------------------------------------------|------|--------------|
| a. Define Linear space and Hilbert space with example. | CO1 | K1 |
| b. Define Linear transformation and Unitary transformation. | CO2 | K1 |
| c. Find $[L_+, L_-]$. | CO3 | K1 |
| d. Obtain the Eigen value of spin $\frac{1}{2}$ particles. | CO4 | K1 |
| e. Mention the properties Pauli spin matrices. | CO5 | K1 |

PART – B**(10 x 5 = 50 Marks)**Answer **ALL** the questions

- | | Marks | CO # | Blooms Level |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|------|--------------|
| 2. a. Discuss about the different operators used in QM and its properties with examples. Prove that for a Hermitian operator, all of its eigen values are real and the eigen vectors corresponding to different eigen values are orthogonal. | 10 | CO1 | K1 |
| (OR) | | | |
| b. State and prove expansion theorem. | 5 | CO1 | K1 |
| c. What are Hermitian Operators? Mention its properties. Show that the Eigen values of Hermitian operators are real. | 5 | CO1 | K1 |
| 3.a. Discuss about the Matrix representation of an Operator? Find the inverse of the matrix: $\begin{bmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{bmatrix}$ | 10 | CO2 | K2 |
| (OR) | | | |
| b. Discuss about the Commutator algebra and all its special properties?. | 10 | CO2 | K2 |
| 4.a. What are the pictures of Quantum Dynamics? Derive the equations of motion in the three pictures. Compare all the three Quantum pictures. | 10 | CO3 | K2 |
| (OR) | | | |
| b. Show that $[L_z, L_+] = \hbar L_+$ and $\vec{L} \times \vec{L} = i\hbar \vec{L}$. | 5 | CO3 | K2 |
| c. Prove that the operators L^2 and L_z commute. | 5 | CO3 | K2 |
| 5.a. Determine the matrix form of L_x, L_y, L_z, L_+, L_- . | 5 | CO4 | K1 |
| b. Determine the Eigen values of L^2 and L_z . | 5 | CO4 | K1 |
| (OR) | | | |
| c. Define total angular momentum operator \mathbf{J} and explain its properties. Obtain the eigen values of \mathbf{J}_z and \mathbf{J}^2 . | 10 | CO4 | K1 |
| 6.a. Explain Pauli spin matrices and their properties with all necessary commutation relations among them. Show that: $(\vec{\sigma} \cdot \vec{A})(\vec{\sigma} \cdot \vec{B}) = \vec{A} \cdot \vec{B} + i\vec{\sigma} \cdot (\vec{A} \times \vec{B})$ | 10 | CO5 | K1 |
| (OR) | | | |
| b. Explain about the Addition of Angular momentum and C. G Coefficient. Find the C. G Coefficient for $J_1 = \frac{1}{2}$ and $J_2 = \frac{1}{2}$ | 10 | CO5 | K3 |

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