



**Gandhi Institute of Engineering and Technology University, Odisha, Gunupur
(GIET UNIVERSITY)**

M.Sc.(First Semester - Regular) Examinations, January – 2026
24MPCMA1104 - Ordinary Differential Equation
(Mathematics)

Time: 3 hrs

Maximum: 60 Marks

**Answer ALL questions
(The figures in the right hand margin indicate marks)**

PART – A

(2 x 5 = 10 Marks)

Q.1. Answer *ALL* questions

- | | CO # | Blooms Level |
|--|------|--------------|
| a. Show that the functions are Lipschitz continues on the given region and find the Lipschitz constant. $f(x, y) = 4x^2 + y^2, x \leq a, y \leq b$ | CO1 | K3 |
| b. Find the general solution of $(x^2D^2 - 4xD + 6)y = 0$ | CO2 | K3 |
| c. Write Bessel's Function | CO3 | K2 |
| d. State the Hille -Wintner Theorem. | CO4 | K2 |
| e. State the Sturm's Comparison theorem | CO5 | K2 |

PART – B

(10 x 5=50 Marks)

Answer ALL the questions

- | | Marks | CO # | Blooms Level |
|--|-------|------|--------------|
| 2. a. Solve by Picard's method of successive approximation
$f(x, y) = e^{-x}y^2 \sin x, 0 \leq y \leq 2, x < 1$ | 5 | CO | K3 |
| b. Show that the functions are Lipschitz continues on the given region and find the Lipschitz constant. $f(x, y) = xy^2$
i. $ x \leq 1, y \leq 1,$
$ x \leq 1, y \leq \infty$
(OR) | 5 | CO1 | K3 |
| c. Find the existence and uniqueness of $f(x, y) = y^{\frac{1}{3}}, y(0) = 0$ | 5 | CO1 | K3 |
| d. Compute the first three approximation for the solution of the equation,
$x' = \frac{x}{1+x^2}, x(0) = 1$ | 5 | CO1 | K3 |
| 3.a. Find the general Solution of $y'' - 9y' + 20y = x + e^{-x}$ | 5 | CO2 | K3 |
| b. Find the general Solution of the system $y_1' = 4y_1 - y_2$ and $y_2' = 2y_1 + y_2$
(OR) | 5 | CO2 | K3 |
| c. Solve the Differential Equation $y'' + 6y' + 9y = \frac{16e^{-3x}}{(x^2+1)}$ | 5 | CO2 | K3 |
| d. Find the general solutions of $x''' + x'' + x' + x = 1$, given that $\cos t, \sin t$ and e^{-t} are three Linear Independent solution of the corresponding homogeneous equation. Also find the solution when $x(0) = 0, x'(0) = 1, x''(0) = 0$. | 5 | CO2 | K3 |
| 4.a. Solve $y'' - y' + xy = 0$ by using power series method | 5 | CO3 | K3 |
| b. Prove that
I. $J_n'(x) = \frac{1}{2} \{J_{n-1}(x) - J_{n+1}(x)\}$
II. $J_{n-1}(x) + J_{n+1}(x) = \frac{2n}{x} J_n(x)$
(OR) | 5 | CO3 | K3 |

- c. Explain Bessel 's Equatio and Bessel's function. 10 CO3 K3
- 5.a. Prove that $J_{-\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \cos x$ 10 CO4 K3
- (OR)
- b. State and prove of Hille -Wintner Theorem 10 CO4 K3
- 6.a. Find the non trivial solution of the sturm -Liouville problem $\frac{d^2y}{dx^2} + \lambda y = 0$ 5 CO5 K3
at $y(0) = 0, y'(1) = 0$
- b. Find the eigenvalues and eigenfunction of the sturm -Liouville problem 5 CO5 K3
 $-4y'' - 4y' + (1 + \lambda)y = 0$ at $y(0) = 0, y'(1) = 0$
- (OR)
- c. Solve the boundary value problem of $u_{tt} = c^2 u_{xx}$, 10 CO5 K3
BCs: $u(0, t) = u(l, t) = 0, \quad 0 \leq x \leq l, \text{ for all } t \geq 0$
 $u(x, 0) = f(x), \quad u_t(x, 0) = g(x), \quad 0 \leq x \leq l.$
- End of Paper ---