



**GANDHI INSTITUTE OF ENGINEERING AND TECHNOLOGY, ODISHA,
GUNUPUR
(GIET UNIVERSITY)**

M.Sc. (First Semester - Regular) Examinations, February - 2025
**24MPHPC11001– MATHEMATICAL METHODS IN PHYSICS
(PHYSICS)**

Time: 3 hrs

Maximum: 60 Marks

Answer ALL questions**(The figures in the right hand margin indicate marks)****PART – A****(2 x 5 = 10 Marks)**Q.1. Answer **ALL** questions

- | | CO # | Blooms Level |
|--|------|--------------|
| a. Define removable isolated singularity. | CO1 | K1 |
| b. Find the value of 'a' for which $f(x, y) = 9x + 6(x^2 - y^2) + 5i(3xy + ay)$ is analytic? | CO1 | K2 |
| c. Write on symmetric tensor. | CO2 | K1 |
| d. Show the graph for Bessel polynomial $J_0(x)$ and $J_1(x)$? | CO4 | K2 |
| e. Write any three properties of gamma functions. | CO6 | K1 |

PART – B**(10 x 5 = 50 Marks)**Answer **ALL** the questions

- | | Marks | CO # | Blooms Level |
|---|-------|------|--------------|
| 2. a. Define Harmonic function. State and Prove Laurent series. | 10 | CO1 | K1 |
| (OR) | | | |
| b. Find the residue of $f(z) = \frac{z}{(2z-4)(3z-5)}$ at $z = \infty$. Explain about different types of singularity. | 10 | CO1 | K1 |
| 3.a. Derive an expression for Direction cosines in Tensor using rectangular coordinate system. | 10 | CO2 | K1 |
| (OR) | | | |
| b. Show that if A_i and B_j are the components of a contravariant and covariant tensor of rank one $C_{ij} = A_i B_j$ are the components of mixed tensor of rank two. | 7 | CO2 | K1 |
| c. Define Christoffel symbol. | 3 | CO2 | K1 |
| 4.a. Prove that the set $\{2^n: n \in \mathbb{Z}\}$ with multiplication operation is an abelian group. | 10 | CO3 | K2 |
| (OR) | | | |
| b. Show that the number of irreducible representation of an Abelian group equals to the number of group elements. | 7 | CO3 | K2 |
| c. Prove that if every element of a group 'G' be its own inverse, then 'G' is abelian. | 3 | CO3 | K1 |
| 5.a. Prove that $\int_{-1}^1 \frac{P_n(x)}{\sqrt{(1-2xt+t^2)}} dx = \frac{2t^n}{2n+1}$ where n is a positive integer. | 10 | CO4 | K2 |
| (OR) | | | |
| b. Evaluate the Legendre polynomials $P_0(x)$, $P_1(x)$, $P_2(x)$ and $P_3(x)$. Show all the Legendre polynomials in a single graph. | 10 | CO4 | K1 |
| 6.a. Evaluate $\int_0^\infty \frac{x^7}{7^x} dx$ | 10 | CO5 | K2 |
| (OR) | | | |
| b. Show that $\int_0^\infty e^{-x^2} dx = \frac{\sqrt{\pi}}{2}$ | 10 | CO5 | K2 |

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