Reg.

No



Time: 3 hrs

GANDHI INSTITUTE OF ENGINEERING AND TECHNOLOGY UNIVERSITY, ODISHA, GUNUPUR (GIET UNIVERSITY)

B. Tech (Fourth Semester - Regular) Examinations, April – 2025 23BCHPC24004 – Numerical Methods in Chemical Engineering

(Chemical Engg.)

Maximum: 60 Marks

AY 23

| Answer ALL questions (The figures in the right-hand margin indicate marks) | | | | | | | |
|---|---------|-------|-----------------|--|--|--|--|
| | x 5 = | 10 Ma | rks) | | | | |
| Q.1. Answer ALL questions | | CO # | Blooms Level | | | | |
| a. What is the Newton -Raphson Method. | | CO1 | K1 | | | | |
| b. Define Upper Triangular Matrix with an example. | | CO2 | K1 | | | | |
| c. Find the Lagrange's interpolating polynomial of the Data $f(0) = 1$, $f(1) = 3$, $f(3) = 55$ | | CO3 | К2 | | | | |
| d. What are the Disadvantages of multistep methods? | | CO4 | K1 | | | | |
| e. Define Difference Quotient. | | CO5 | K1 | | | | |
| $\mathbf{PART} - \mathbf{B}$ |) x 5 = | 50 Ma | arks) | | | | |
| Answer ALL the questions | Marks | CO # | Blooms | | | | |
| 2. a. Solve the system | | | Level | | | | |
| x+y+2z=4, $2x-y+3x=9$, $3x-y-z=2$ by LU Decomposition Method. | 5 | CO1 | К2 | | | | |
| b. Find a real root of $x^3 - x - 1 = 0$, by Fixed Point Iteration Method | 5 | CO1 | К2 | | | | |
| (OR) | | | | | | | |
| c. Solve $10x+2y+z=9$, | | | | | | | |
| x+10y-z=-22, | 10 | CO1 | K2 | | | | |
| -2x+3y+10z=22 By Gauss -Seidel Method. | | | | | | | |
| 3.a. Using the following data, Estimate the value of $f(-0.5)$ & $f(0.5)$ by Hermite | | | | | | | |
| Interpolation. | | | | | | | |
| $\begin{array}{c ccc} x & f(x) & f^{1}(x) \\ \hline \end{array}$ | 10 | C02 | K2 | | | | |
| -1 1 -5 1 1 | | | | | | | |
| | | | | | | | |
| 1 3 7 (OR) | | | | | | | |
| b. Obtain the piecewise linear interpolation for the function $f(x)$. Also find $f(7)$. | | | | | | | |
| X 1 2 4 8 | 5 | CO2 | КЗ | | | | |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | | | | | | |
| c. Find the Lagrange's quadratic interpolating polynomial for the data, | | | | | | | |
| | | | | | | | |
| x 0 1 3 | 5 | CO2 | КЗ | | | | |
| y 1 3 5.5 | | | | | | | |
| 4.a. From the following table find $f^{\dagger}(3)$ by using By Richardson's extrapolation. | | | | | | | |
| x -1 1 2 3 4 5 7 | 5 | CO3 | КЗ | | | | |
| F(x) 1 1 16 81 251 625 2401 | | | | | | | |

| b. | Find the Jacobian matrix for the following system $F_1 = x^2+y^2-x = 0$ $F_2 = x^2-y^2-y = 0$ at point (2,2) with h=k=1. (OR) | 5 | CO3 | К3 |
|------|---|---|-----|----|
| c. | Evaluate $I=\int_0^1 \frac{1}{1+x} dx$ by Simpson's rule & Romberg's Method with n=10 | 5 | CO3 | К3 |
| d. | Find $f^1(\prod/4)$ with $h = (\prod/12)$ Given $f(x) = \sin x$, by using Backward difference formula | 5 | CO3 | КЗ |
| 5.a. | Evaluate y (2), if y(x) is the solution of $y^1(x) = (x+y)$ given y (0) =1 by using Adams Moulton method of 3^{rd} order | 5 | CO4 | КЗ |
| b. | Evaluate y (2), given $y^1(x)=0.5(x+y) \& y(0)=2$ by Adams Bash forth method of order 4. | 5 | CO4 | КЗ |
| | (OR) | | | |
| c. | Estimate y (0.4), for the initial value problem $y^1 = -2xy^2$ & y (0) =1 by Adams bash- forth predictor –corrector formula | 5 | CO4 | КЗ |
| d. | Using Runge –Kutta Method (R-K method) find y (0.2), Given $y^1 = x + y$, $y(0) = 1$ | 5 | CO4 | K3 |
| 6.a. | Solve $U_{xx} = U_t$ given $U(0, t) = 0$ & $U(1, t) = t$ & $U(x, 0) = \sin \pi x$. By Bender-Schmidt formula. find the values of U up to t=5. assume h=k=1 | 5 | CO5 | КЗ |
| b. | Explain about the Method of solution for Laplace Equation. (OR) | 5 | CO5 | КЗ |
| c. | Solve the equation $U_{xx} = U_t$ subject to U (x,0) =0, U (0, t) = 0 & U (1, t) =t for two-time steps with h=1, by Crank –Nicholson Method. | 5 | CO5 | КЗ |
| d. | Solve $4U_{xx} = U_t$. Given u (0, t) =0; u (4, t) =0 with initial condition u(x,0) =x(4- x) and u _t (x,0) =0; Assume h=1/4, find the values of u up to one step in t. End of Paper | 5 | CO5 | K3 |