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**GANDHI INSTITUTE OF ENGINEERING AND TECHNOLOGY, ODISHA,
GUNUPUR
(GIET UNIVERSITY)**

B. Tech (Second Semester – Regular/Supplementary) Examinations, April – 2025
23BBSBS12001 - Engineering Mathematics-II
(BIOTECH)

Time: 3 hrs

Maximum: 60 Marks

Answer ALL questions

(The figures in the right hand margin indicate marks)

PART – A**(2 x 5 = 10 Marks)**Q.1. Answer **ALL** questions

- | | CO # | Blooms
Level |
|--|------|-----------------|
| a. Find the distance between the points (2,3) and (4,5). | CO1 | K1 |
| b. Find $\lim_{x \rightarrow 0} \frac{\sqrt{5+x} - \sqrt{5-x}}{x}$ | CO1 | K2 |
| c. Find the integration of $\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$ | CO1 | K2 |
| d. What is the probability of getting a sum of 9 when two dice are thrown? | CO1 | K1 |
| e. Find the gradient of F where i. $F = e^{xyz}$ ii. $F = x^2 + y^2 + z^2$. | CO2 | K2 |

PART – B**(10 x 5 = 50 Marks)**Answer **ALL** the questions

- | | Marks | CO # | Blooms
Level |
|---|-------|------|-----------------|
| 2. a. Find the angle between two lines $y = x$ and $y = -x$. | 5 | CO2 | K2 |
| b. Find the equation of circle passing through the points (3,4), (3,2) and (1,4). | 5 | CO2 | K2 |
| (OR) | | | |
| c. Find the equation of circle passing through the points (2,3) and (4,5) and also find its centre and radius. | 5 | CO2 | K2 |
| d. Show that A (-2,7), B (1,1) C(3,-3) are collinear. | 5 | CO2 | K2 |
| 3.a. Find the derivative of i. $e^{\sqrt{\sin x}} + e^{\sqrt{\cos x}}$ ii. $\log \sqrt{\sin x} + \log \cos x$ | 5 | CO2 | K2 |
| b. Find the derivative of i. $(x^2 + 2x - 1)^5$ ii. $\cos(\ln x)^2$ | 5 | CO3 | K3 |
| (OR) | | | |
| c. Find the limit of i. $\lim_{x \rightarrow 1} \frac{2x^3 - 3x^2 + 1}{9x^2 + 8x + 7}$ ii. $\lim_{x \rightarrow 0} \frac{\sqrt{5+x} - \sqrt{5-x}}{x}$ | 5 | CO2 | K3 |
| d. Find the derivative of i. $\frac{\sin x}{e^x}$ ii. $\frac{1 - \tan x}{1 + \tan x}$ | 5 | CO3 | K3 |
| 4.a. Find the integration i. $\int \frac{x^3 + 3x + 4}{\sqrt{x}} dx$ ii. $\int \frac{x^3 + 5x^2 - 4}{x^2} dx$ | 5 | CO3 | K3 |
| b. Find the integration of i. $\int 2x\sqrt{1+x^2} dx$ ii. $\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$ | 5 | CO3 | K3 |
| (OR) | | | |
| c. Find the integral of i. $\int x \sin x dx$ ii. $\int x \cos x dx$ | 5 | CO2 | K3 |
| d. Find the area under the curve $f(x) = x^2 - 2x + 2$ from $x=1$ to $x=2$ | 5 | CO3 | K3 |
| 5.a. In a factory that produces bolts, three machines A, B, and C are responsible for manufacturing 25%, 35%, and 40% of the total bolts, respectively. The defect rates of these machines differ: machine A produces 5% defective bolts, machine B produces 4% defective bolts, and machine C produces 2% defective bolts. A | 5 | CO2 | K2 |

bolt is randomly selected from the overall production, and it is found to be defective. What is the probability/likelihood that this defective bolt was produced by machine B?

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|------|--|---|-----|----|
| b. | Two dice are rolled, find the probability that the sum of the number of both the dice is i) Equal to 2 ii) Equal to 5 iii.) Less than 12 | 5 | CO3 | K2 |
| (OR) | | | | |
| c. | State and Prove Bayes Theorem. | 5 | CO2 | K2 |
| d. | If $P(A)=0.8$ $P(B)=0.5$, $P\left(\frac{B}{A}\right) = 0.4$ then Find i. $P(A \cap B)$ ii. $P(A \cup B)$ iii. $P(A B)$ | 5 | CO3 | K2 |
| 6.a. | Find the directional derivative of a function $f = x^2 + 3y^2 + 4z^2$ in the direction of a vector $(1, -1, -1)$ at a point $(1,0,1)$. | 5 | CO3 | K2 |
| b. | Find the angle between two normal surfaces $x^2 + y^2 + z^2 = 10$ and $x^2 + 2y^2 + 3z^2 = 15$ at point $P(2,3,4)$. | 5 | CO2 | K2 |
| (OR) | | | | |
| c. | Find the angle between the vectors \vec{a} and $\vec{b} + \vec{c}$. Where $\vec{a} = \hat{i} + \hat{j}$, $\vec{b} = 3\hat{i} + 2\hat{j} + 3\hat{k}$ and $\vec{c} = \hat{i} + 2\hat{j}$. | 5 | CO3 | K2 |
| d. | Find i. $\text{Curl}(\text{grad} f)$ ii. $\text{div}(\text{curl} f)$. | 5 | CO3 | K3 |

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