



B. Tech (First Semester - Regular) Examinations, December – 2024 23BBSBS110B1 - Engineering Mathematics- I

(Only for Biotech)

Maximum: 60 Marks

| (The figures in the right hand margin indicate marks) | | | | | | | |
|---|--|-----------|-----------------|--|--|--|--|
| | | 10 Marks) | | | | | |
| Q.1. | . Answer ALL questions | CO # | Blooms Level | | | | |
| a. | Use a direct proof to show that the sum of two even integers is even | CO1 | K1 | | | | |
| b. | Let $A = \{1, 2, 3, 4\}$. Find the relation R is | | | | | | |
| | a. Reflexive with Symmetric | CO2 | K2 | | | | |
| | b. Reflexive with Transitive | | | | | | |
| c. | Define the Diagonally Dominance of linear equation | CO2 | K1 | | | | |
| d. | Find the Relative error and Percentage error of the point $x_T = 2.3456789$, $X_A = 2.33$ | CO1 | K1 | | | | |
| e. | Find the mean, median, and mode of the given data are | CO3 | K 1 | | | | |
| | 8, 11, 4, 3, 2, 5, 10, 6, 4, 1, 10, 8, 12, 6, 5, 7. | 005 | КI | | | | |

Answer ALL questions

| PART | – B |
|------|------------|
| IANI | - D |

Time: 3 hrs

(10 x 5 = 50 Marks)

| Answer ALL the questions | | CO # | Blooms Level |
|--|---|------|-----------------|
| 2. a. Show that $(p \to q) \lor (p \to r)$ and $p \to (q \lor r)$ are logically equivalent | 5 | CO2 | K2 |
| b. Prove that $1^3 + 2^3 + 3^3 \cdots + n^3 = \left[\frac{n(n+1)}{2}\right]^2$ for the positive integer n by Using mathematical induction. | 5 | CO2 | К3 |
| (OR) | | | |
| c. Construct the truth table of $(p \lor q) \land (p \to r) \land (q \to r)$. | 5 | CO2 | K2 |
| d. Show that $\sqrt{2}$ is a irrational number by method of contradiction | 5 | CO2 | К3 |
| 3.a. Find the inverse of the matrix $A = \begin{pmatrix} 2 & 3 & 4 \\ 4 & 3 & 1 \\ 1 & 2 & 4 \end{pmatrix}$ | 5 | CO2 | K2 |
| b. Solve the system of linear equation by Cramer's Rule 3x + 2y + 4z = 18, $x - 2y + 5z = 15$, $2x + 6y + 7z = 11$ | 5 | CO3 | К3 |
| (OR) | | | |
| c. Find the rank of the matrix $\begin{bmatrix} 3 & -1 & 3 \\ 2 & -4 & 6 \\ 10 & 0 & 14 \end{bmatrix}$ | 5 | CO3 | K2 |
| d. Solve the system of linear equation by Cramer's Rule 5x - 3y + z = 6, $2x + 3y - z = 8$, $8x + 9y - 3z = 28$ | 5 | CO4 | К3 |
| 4.a. Find root of equation $\cos x - 3x + 1 = 0$ by using Newtown- Raphson method up to three decimal | 5 | CO4 | K2 |
| b. Solve the system of Linear equations, by Gauss elimination method | 5 | CO4 | К3 |

| | x + 5y - z = 10, x + y + 8z = 20, 4x + 2y + z = 14 (OR) | | | |
|------|--|---|-----|----|
| c. | Find root of equation $x^3 - 3x + 1 = 0$ by using Iteration method up to three decimal. | 5 | CO3 | К2 |
| d. | Solve the Linear equations, by Gauss – Seidel method up to two decimal | | | |
| | 10x + 2y + z = 9 | 5 | CO4 | КЗ |
| | x + 10y - z = -22 | | | |
| 5 | -2x + 3y + 10z = 22 | | | |
| 5.a. | Find the value $f(9)$ given data by using Newton forward interpolation formula | _ | | |
| | x 8 10 12 14 16 18 | 5 | CO5 | К2 |
| | f(x) 10 19 32.5 54 89.5 15.4 | | | |
| b. | Obtain the Newton's divided difference interpolating polynomial and find $f(3)$ | | | |
| | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 5 | CO5 | КЗ |
| | | | | |
| | (OR) | | | |
| c. | Find the interpolation polynomial of given data and find $y(3.5)$ and $y(5.5)$. | | | |
| | x 3 4 5 6 | 5 | CO5 | КЗ |
| | $Y = f(x) \qquad 6 \qquad 24 \qquad 60 \qquad 120$ | | | |
| d. | Find the value of $y(4)$ by Using Lagrange's interpolation formula of the | | | |
| | following data | 5 | CO5 | КЗ |
| | x -1 0 2 3 5 Y = f(x) -8 3 1 2 43 | | | |
| 6.a. | Out of 100 numbers, 20 were 4's, 40 were 5's, 30 were 6's and the remainder | | | |
| 0.4 | were 7's. Find the arithmetic mean of the numbers and its standard deviation. | 5 | CO4 | К2 |
| b. | Find a least squares straight line of Y on X for the given data: Predict Y at $X =$ | | | |
| | 5 | 5 | CO4 | КЗ |
| | X 2 4 6 8 10 12 | J | 004 | ĸJ |
| | Y 1.8 1.5 1.4 1.1 1.1 0.9 | | | |
| - | (OR) | | | |
| c. | Four groups of students, consisting of 15, 20, 10, and 18 individuals, reported mean weights of 162, 148, 153, and 140 pounds (lb), respectively. Find the | 5 | CO5 | К2 |
| | mean weight of all the students and its variance. | J | 05 | ĸΖ |
| d. | Determine the correlation coefficient for the correct . | | | |
| | X 1 2 3 4 5 6 | 5 | CO4 | КЗ |
| | Y 6 4 3 5 4 2 | | | |

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