

GANDHI INSTITUTE OF ENGINEERING AND TECHNOLOGY UNIVERSITY, ODISHA, GUNUPUR (GIET UNIVERSITY)



Ph.D. (First Semester) Examinations, December - 2024 23SPPEMT1011/ SPPEMT1011 - Computational Mathematics (Mathematics)

Time: 3 hrs Maximum: 70 Marks

The figures in the right hand margin indicate marks.

Answer ANY FIVE Questions.

 $(14 \times 5 = 70 \text{ Marks})$ Marks

6

9

5

7

- 1.a. Solve the differential equation using Laplace Transform 4 y'' -4y' +37 y = 0, y(0)=3, y'(0)=10
- b. Find the interpolating polynomial by using Newton divided difference formula for the following data:

X	-1	0	2	3
F(x)	-8	3	1	12

- 2. Transform the equation to normal form and solve it. $U_{xx} 2 U_{xy} + U_{yy} = 0$ 14
- 3. Derive the two-step Adams-Bashforth method by using Taylor's theorem 14
- 4. Derive the D'Alembert's solution of the one dimensional wave equation.
- 5.a. Solve the system of equations by using Comparison method 3x 2y = 2, 7x + 3y = 43
- b. Find the value of f(x) at x=15 from the following table

X	4	5	7	10	11	13
f(x)	48	100	294	900	1210	2028

- 6.a. Derive the Trapezoidal formula.
- b. Explain about implicit and explicit of a function with example.
- 7. Solve the differential equation using Laplace Transform $y'' + 9 y = \sin t$ if $0 < t < \pi$, and 0 14 if $t > \pi$, y(0) = 0 and y'(0) = 4
- 8.a. Find the value of $\int_0^\infty \sqrt{y} e^{-y^2} dy$
 - b. Find the solution of the differential equation $y' = x^2 y^2$ in the range 0 < x < 2 for the boundary condition y=0 at x=0 (Apply Milne's method)

---End of Paper---